

トポロジカル超伝導体としてのUPt₃

理研

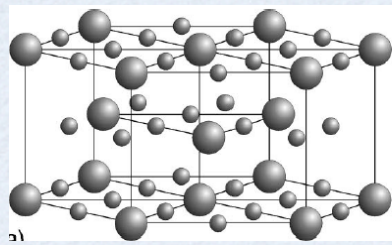
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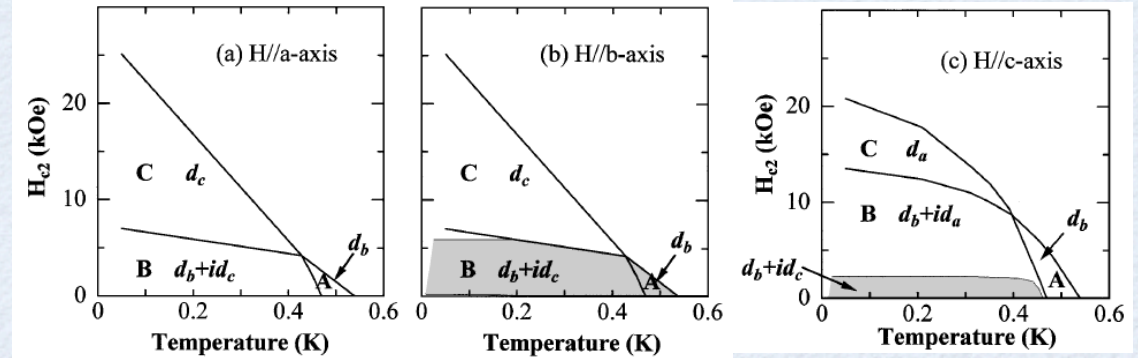
Superconductivity in UPt_3

Crystal structure



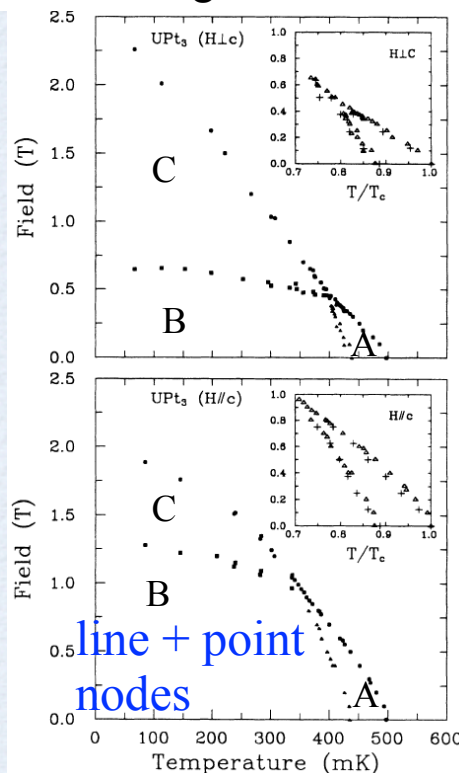
U
 Pt
 D_{6h}
 hexagonal

NMR Knight shift



H. Tou *et al.*, PRL **80**, 3129 (1998).

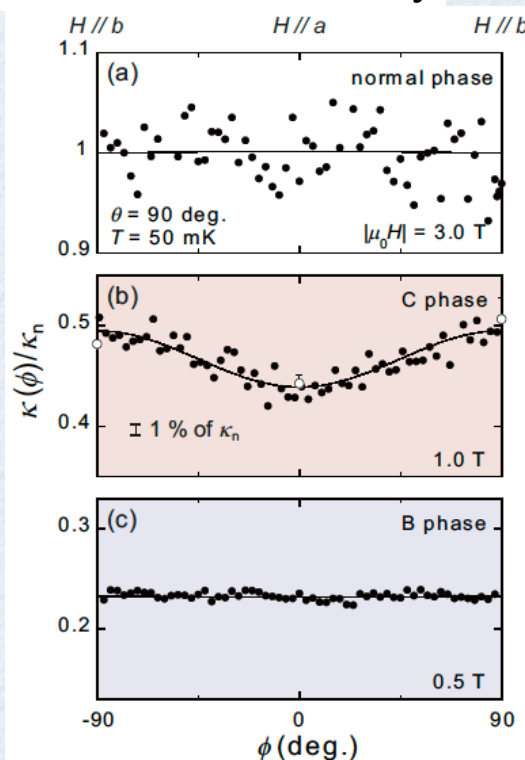
Phase diagram



line + point nodes

S. Adenwalla *et al.*, PRL **65**, 2298 (1990).

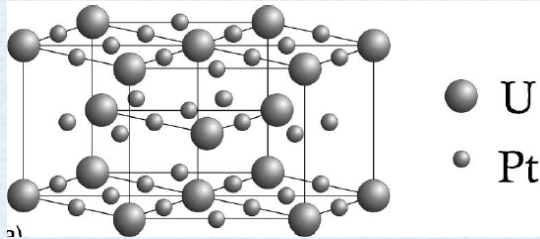
Thermal conductivity



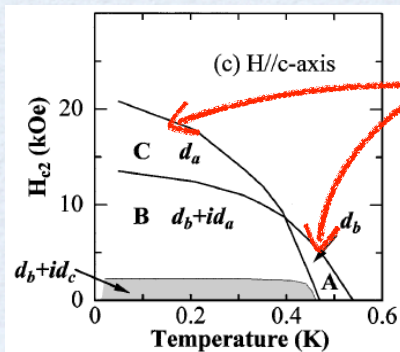
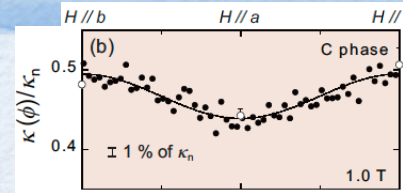
- line + point nodes in B phase
- spin-triplet
- twofold symmetry in C phase

Y. Machida *et al.*, PRL **108**, 157002 (2012).

Gap function



D_{6h}
hexagonal



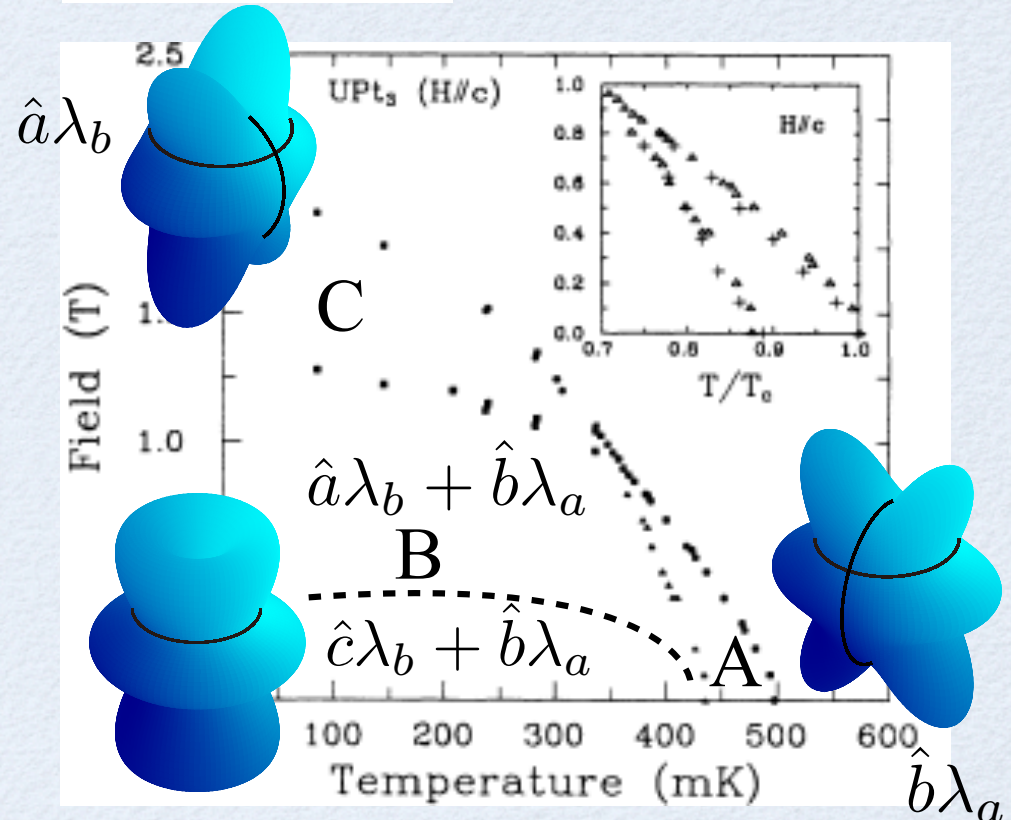
2次元表現

- line + point nodes
- twofold symmetry

f-wave: $Y_3^{\pm 1}(\theta, \phi) \propto \sin \theta (5 \cos^2 \theta - 1) e^{\pm i\phi}$

E_{1u} representation

$$\lambda_a = k_a(5k_c^2 - 1), \quad \lambda_b = k_b(5k_c^2 - 1)$$



Y. Tsutsumi *et al.*, JPSJ **81**, 074717 (2012).

B phase: unitary state

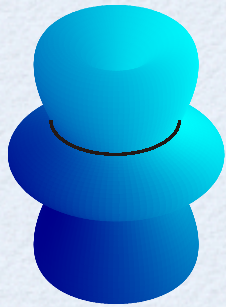
$$k_c = \pm 1/\sqrt{5}$$

tropical line nodes: $\theta \approx 66^\circ, 114^\circ$

Topological aspect

UPt₃ B phase

$$(\hat{b}k_a + \hat{c}k_b)(5k_c^2 - 1)$$

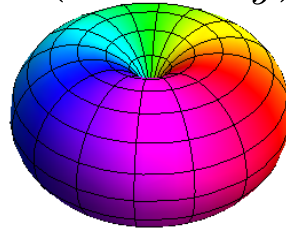


helical state
point nodes
tropical line nodes

- edge state
- vortex core state

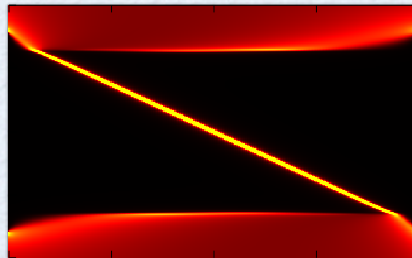
³He A-phase

$$\hat{z}(k_x + ik_y)$$



chiral superfluid

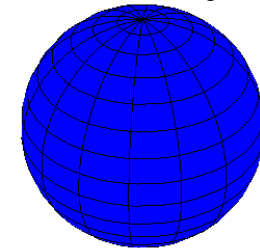
Edge state



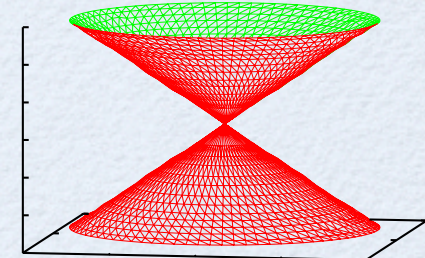
mass current

³He B-phase

$$\hat{x}k_x + \hat{y}k_y + \hat{z}k_z$$

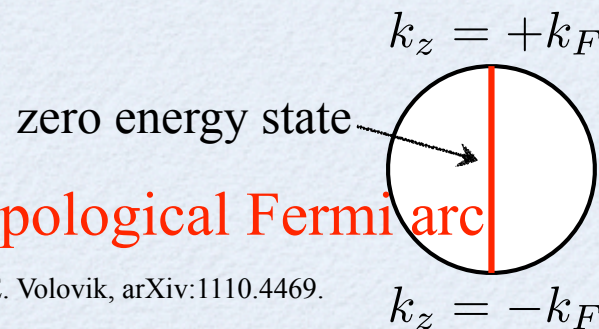


helical superfluid

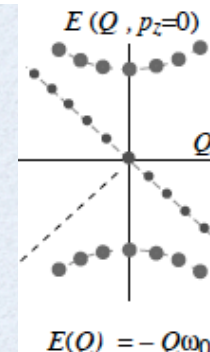


Majorana cone
spin current

Vortex core state



G. E. Volovik, arXiv:1110.4469.



normal core vortex

Majorana
zero energy mode

G. E. Volovik

Quasi-classical Eilenberger theory

$$\Delta/E_F \ll 1 \quad \int d\xi_k \hat{\sigma}_z \hat{G}(\mathbf{k}, \mathbf{r}, \omega_n) \equiv \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) \equiv -i\pi \begin{pmatrix} \hat{g} & i\hat{f} \\ -i\hat{f} & -\hat{g} \end{pmatrix}$$

Eilenberger equation

$$-i\hbar \mathbf{v}_F \cdot \nabla \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) = \left[\begin{pmatrix} i\omega_n \hat{1} & -\hat{\Delta}(\mathbf{k}_F, \mathbf{r}) \\ \hat{\Delta}^\dagger(\mathbf{k}_F, \mathbf{r}) & -i\omega_n \hat{1} \end{pmatrix}, \hat{g}(\mathbf{k}_F, \mathbf{r}, \omega_n) \right]$$

$$\hat{g} \downarrow \quad \uparrow \hat{\Delta}$$

Gap equation

$$\hat{\Delta}(\mathbf{k}_F, \mathbf{r}) = N_0 \pi k_B T \sum_{-\omega_c \leq \omega_n \leq \omega_c} \left\langle V(\mathbf{k}_F, \mathbf{k}'_F) \hat{f}(\mathbf{k}'_F, \mathbf{r}, \omega_n) \right\rangle_{\mathbf{k}'_F}$$

Current

$$\mathbf{j}_0^\mu(\mathbf{r}) = j_0^\mu \pi k_B T \sum_{\omega_n} \langle \mathbf{v}_F \text{Im}[g_\mu(\mathbf{k}_F, \mathbf{r}, \omega_n)] \rangle_{\mathbf{k}_F}$$

$$\hat{g} = \begin{pmatrix} g_0 + g_z & g_x - ig_y \\ g_x + ig_y & g_0 - g_z \end{pmatrix}$$

$\mu = 0$: charge current

$\mu = x, y, z$: spin current of μ -spin

Local density of states (LDOS)

$$N(\mathbf{r}, E) = \langle N(\mathbf{k}_F, \mathbf{r}, E) \rangle_{\mathbf{k}_F} = N_0 \langle \text{Re}[g_0(\mathbf{k}_F, \mathbf{r}, \omega_n)|_{i\omega_n \rightarrow E+i\eta}] \rangle_{\mathbf{k}_F}$$

Dispersion

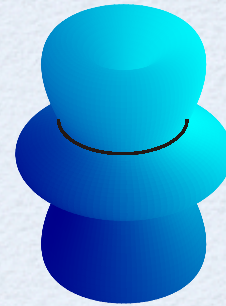
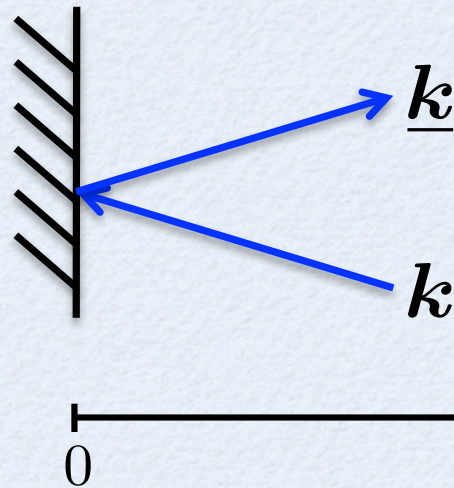
Calculation of edge state

specular edge

$$\hat{g}(\mathbf{k}, a = 0, \omega_n) = \hat{g}(\underline{\mathbf{k}}, a = 0, \omega_n)$$

$$\mathbf{k} = (k_a, k_b, k_c)$$

$$\underline{\mathbf{k}} = (-k_a, k_b, k_c)$$



$$\hat{\Delta} = \Delta_0(\hat{b}k_a + \hat{c}k_b)(5k_c^2 - 1)$$

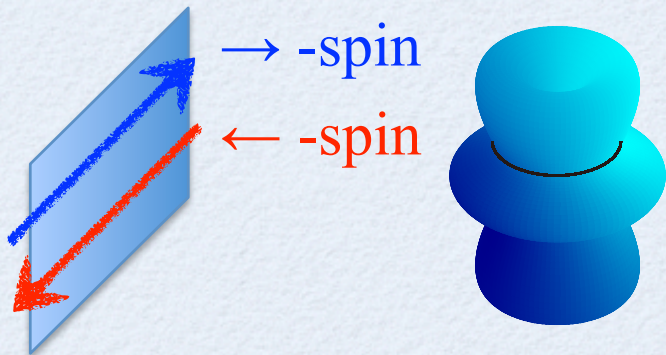
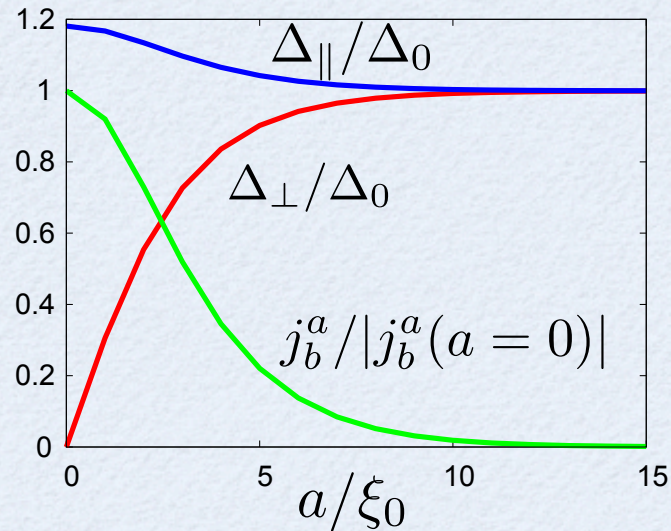
a

Result of edge state

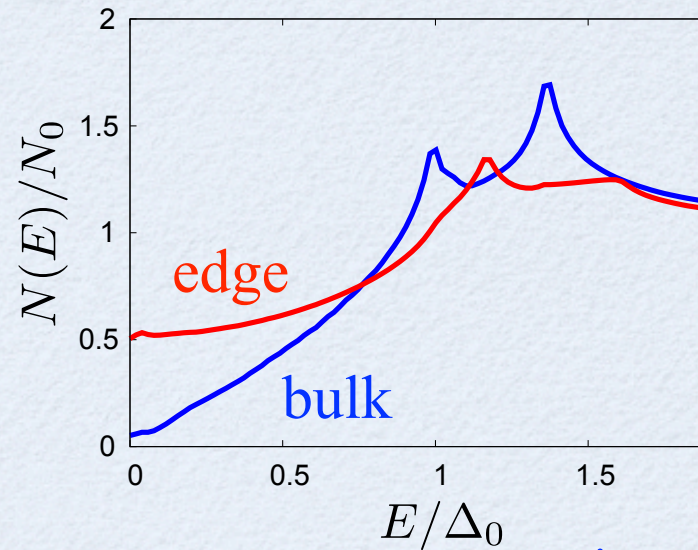
$$\hat{\Delta}(a, \mathbf{k}) = (\Delta_{\perp}(a)\hat{b}k_a + \Delta_{\parallel}(a)\hat{c}k_b)(5k_c^2 - 1)$$

$$\Delta_{\perp, \parallel}(a \rightarrow \infty) = \Delta_0$$

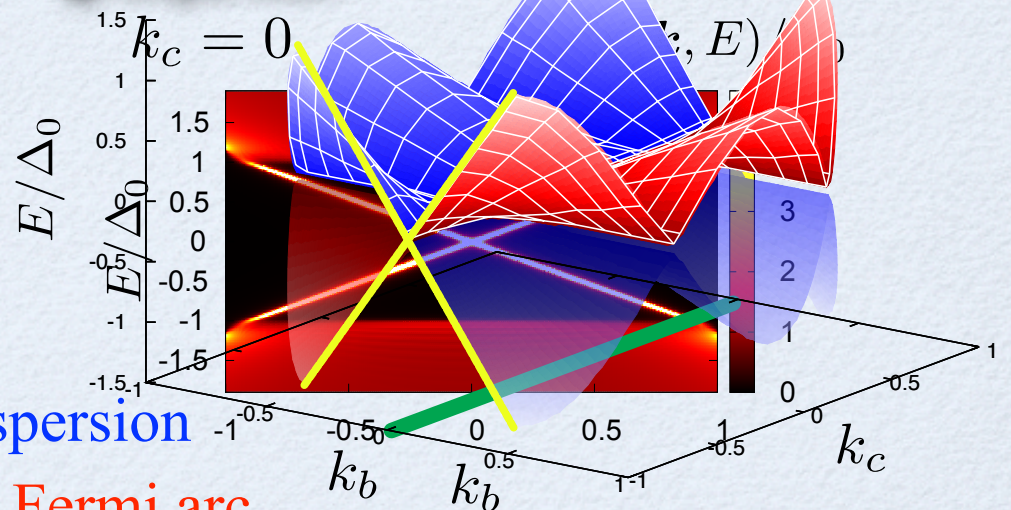
order parameter and spin current



LDOS



dispersion



linear dispersion
topological Fermi arc

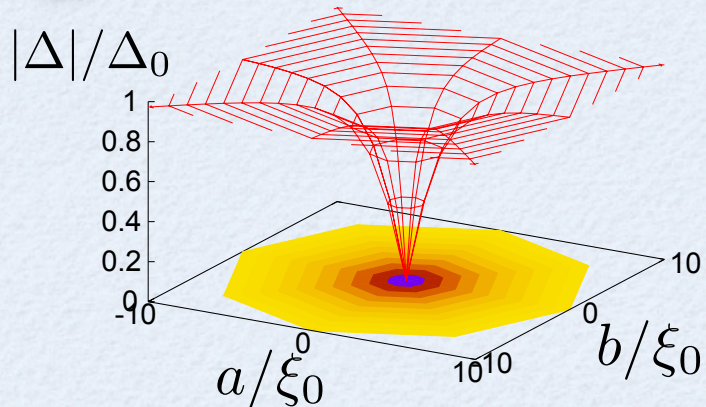
Calculation of vortex state

$$\hat{\Delta}(\mathbf{r}, \mathbf{k}) = \Delta(\mathbf{r})(\hat{b}k_a + \hat{c}k_b)(5k_c^2 - 1)$$

vortex // c -axis

$$\Delta(\mathbf{r} \rightarrow \infty) = \Delta_0 e^{i\phi}$$

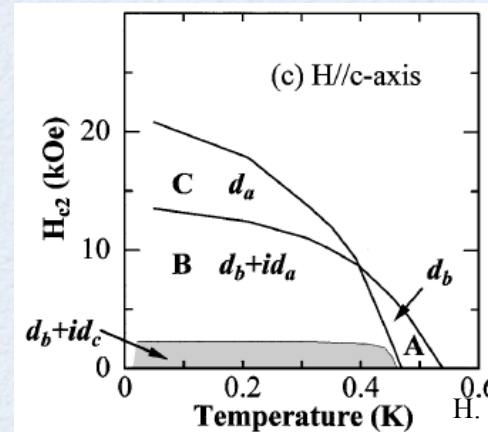
 **normal-core vortex**



Bogoliubov-de Gennes theory

$$\int d\mathbf{r}_2 \begin{pmatrix} H_0(\mathbf{r}_1, \mathbf{r}_2) & \Delta(\mathbf{r}_1, \mathbf{r}_2) \\ -\Delta(\mathbf{r}_1, \mathbf{r}_2)^* & -H_0^*(\mathbf{r}_1, \mathbf{r}_2) \end{pmatrix} \begin{pmatrix} u(\mathbf{r}_2) \\ v(\mathbf{r}_2) \end{pmatrix} = E \begin{pmatrix} u(\mathbf{r}_1) \\ v(\mathbf{r}_1) \end{pmatrix}$$

$u = v^*$: **Majorana zero energy mode**



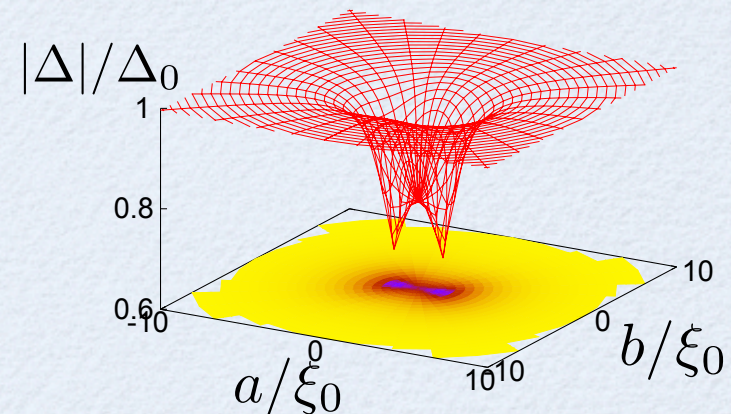
H. Tou *et al.*, PRL **80**, 3129 (1998).

 **double-core vortex**

$$\Delta_a \hat{a}k_b(5k_c^2 - 1)$$

stable in low- T & low- H region

Y. Tsutsumi *et al.*, JPSJ **81**, 074717 (2012).

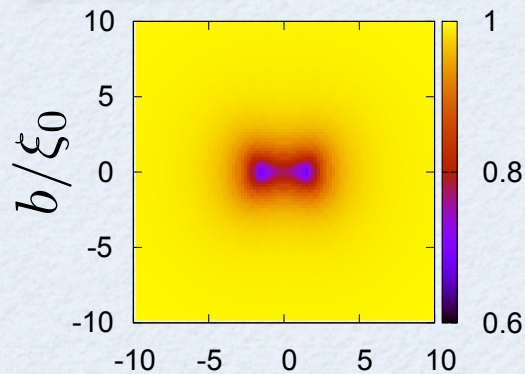


Result of vortex state

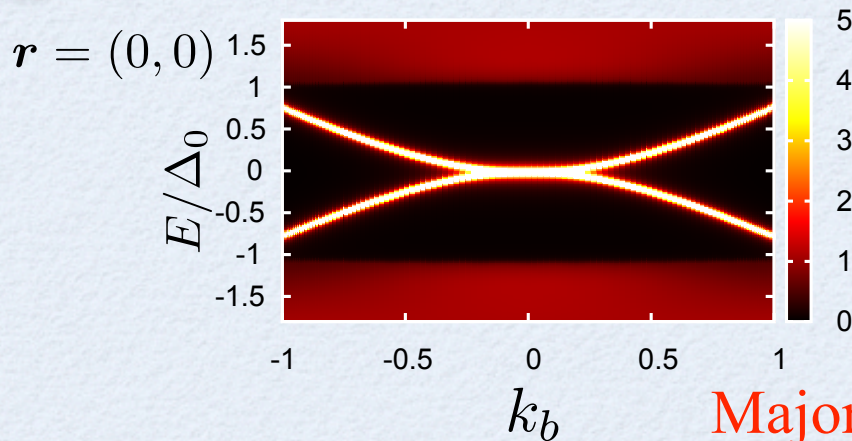
bulk: $\Delta_{bc}(\hat{b}k_a + \hat{c}k_b)(5k_c^2 - 1)$

vortex core: $\Delta_a \hat{a}k_b(5k_c^2 - 1)$

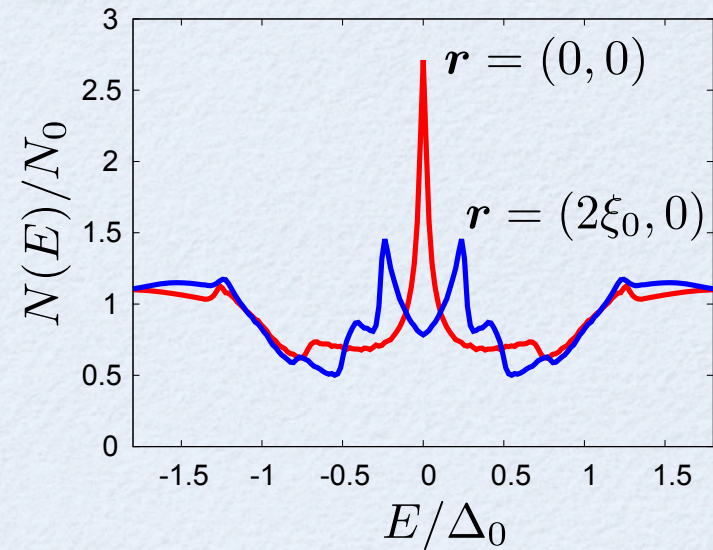
order parameter $|\Delta|/\Delta_0$



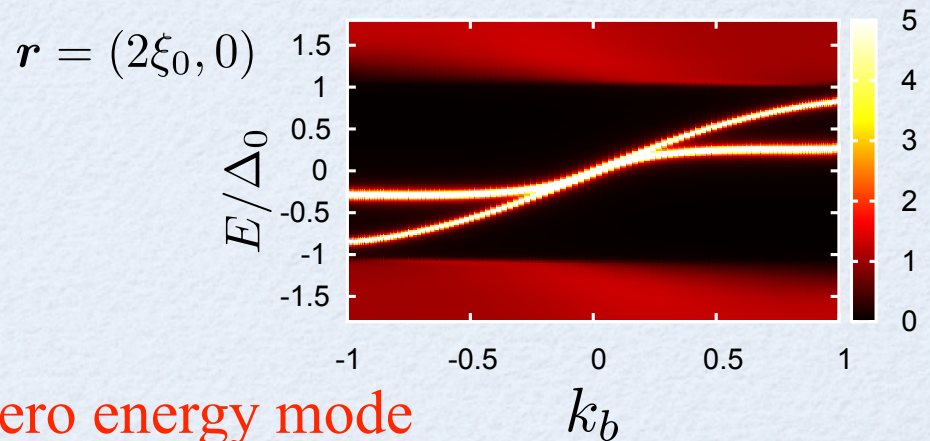
dispersion $k_c = 0$ $N(\mathbf{k}, E)/N_0$



LDOS

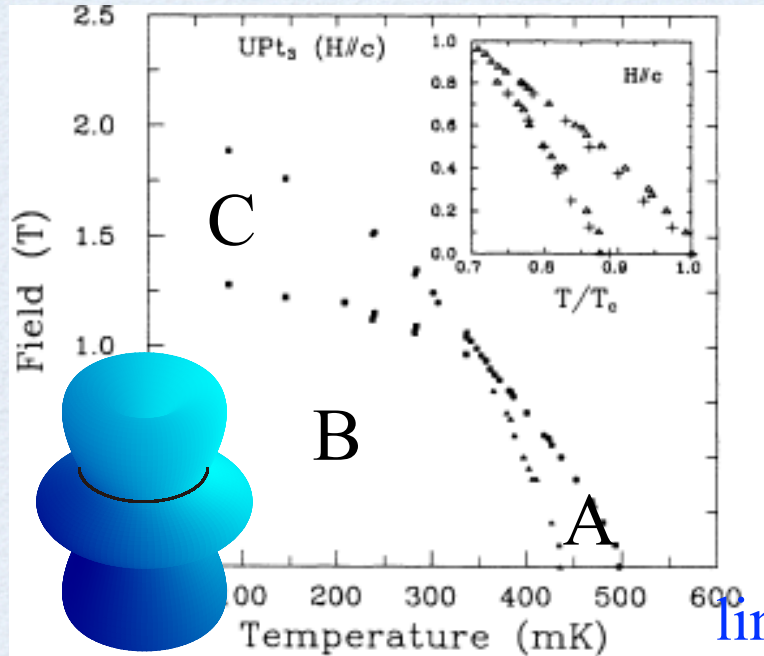


$N(\mathbf{k}, E)/N_0$



Majorana zero energy mode

Summary

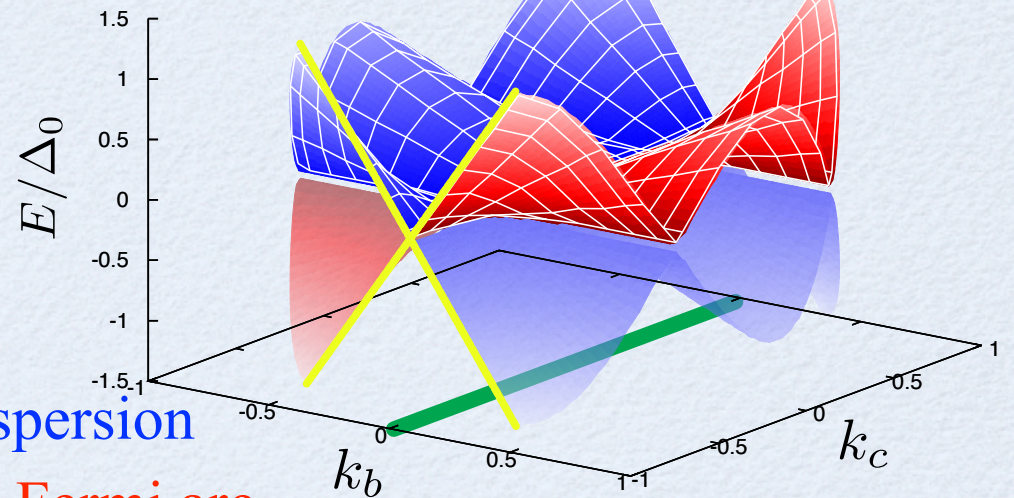


Edge state

spin current

→ -spin

← -spin



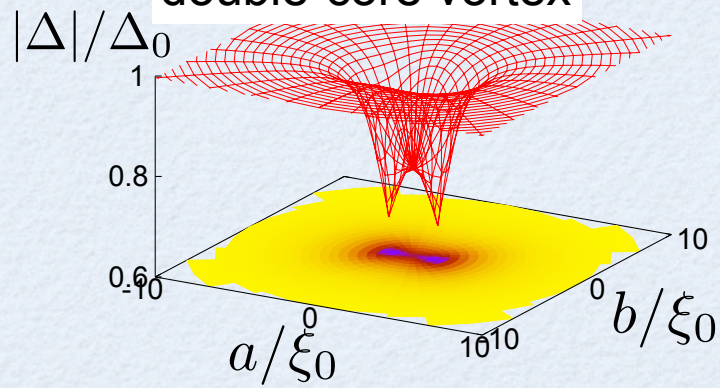
$$(\hat{b}k_a + \hat{c}k_b)(5k_c^2 - 1)$$

topological Fermi arc



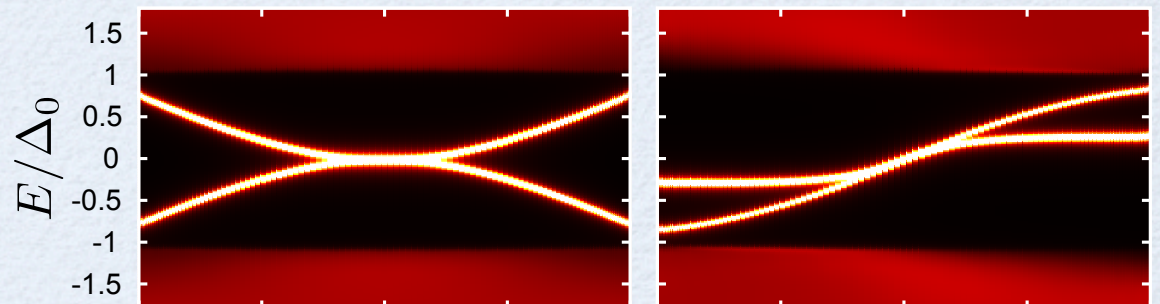
Vortex state

double-core vortex



$$\mathbf{r} = (0, 0)$$

$$\mathbf{r} = (2\xi_0, 0)$$



Majorana zero energy mode